**Year 12 Examination, 2019**

**Question/Answer Booklet**

**MATHEMATICS SPECIALIST**

**Section One: Calculator-free**

Student Name/Number: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Teacher Name: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Time allowed for this section**

Reading time before commencing work: five minutes

Working time for this section: fifty minutes

**Materials required/recommended for this section**

**To be provided by the supervisor:** This Question/Answer Booklet

Formula Sheet

**To be provided by the candidate:**

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters

Special items: nil

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

**Structure of this paper**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of exam |
| Section One: Calculator-free | 8 | 8 | 50 | 50 | 35 |
| Section Two: Calculator-assumed | 10 | 10 | 100 | 100 | 65 |
|  | | | | | 100 |

**Instructions to candidates**

1. The rules for the conduct of School exams are detailed in the *\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_School/College assessment policy*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet preferably using a blue/black pen. Do not use erasable or gel pens.
3. You must be careful to confine your answer to the specific question asked and to follow any instructions that are specified to a particular question.
4. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
5. It is recommended that you do not use pencil, except in diagrams.
6. Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

**Section One: Calculator-free 35% (50 Marks)**

This section has **eight** questions. Answer **all** questions. Write your answers in the spaces provided.

Supplementary pages for planning/continuing your answers to questions are provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.

Working time: 50 minutes.

**Question 1 (4 marks)**

The complex number .

(a) Show that  is purely imaginary. (3 marks)



(b) Determine the least positive number  such that  is real. (1 mark)

**Question 2 (10 marks)**

Consider the system of equations



in which and  are constants.

(a) Write this system in augmented matrix form. (1 mark)

(b) Reduce this augmented matrix to echelon form. (3 marks)

(c) Hence deduce the value(s) of ** and ** for which the system of equations possesses

(3 marks)

1. a unique solution
2. no solutions
3. infinitely many solutions

(d) Determine the general solution of the system of equations when it admits an infinity of solutions. (3 marks)

**Question 3 (5 marks)**

Suppose that the linear function is its own inverse.

Determine all possible values of the constants and .

**Question 4 (4 marks)**

If is any non-zero complex number, prove that

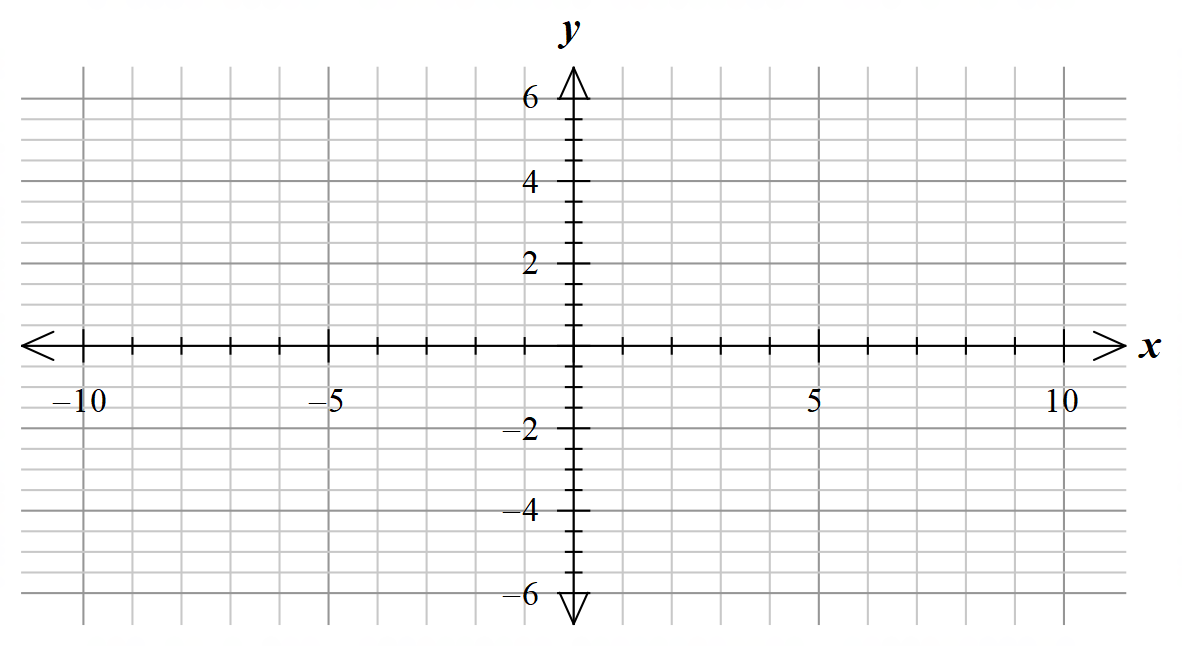
.

**Question 5 (6 marks)**

Suppose that .

(a) For which real numbers is defined? (3 marks)

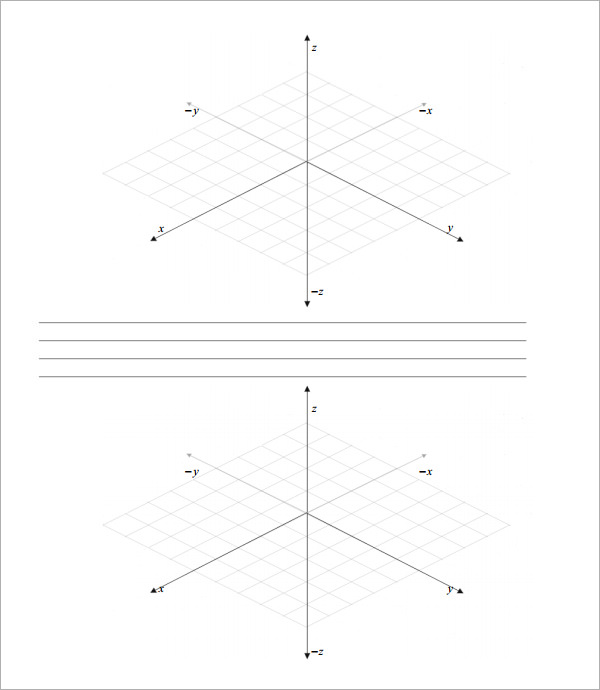
(b) Sketch on the axes below the graph of . (3 marks)



**Question 6 (9 marks)**

Suppose that *Q* is the plane defined by the equation .

(a) Sketch the triangle whose vertices are the and intercepts of the plane. (2 marks)



(b) Show that the point P= lies on *Q.* (1 mark)

(c) Show that the vector **v****i****j****k** is perpendicular to *Q.*  (2 marks)

(d) Write down the Cartesian equation of the plane *R* that is parallel to *Q* and which contains the point . (2 marks)

(e) Determine a vector **w** that is perpendicular to both OP and **v**. (2 marks)

**Question 7 (6 marks)**

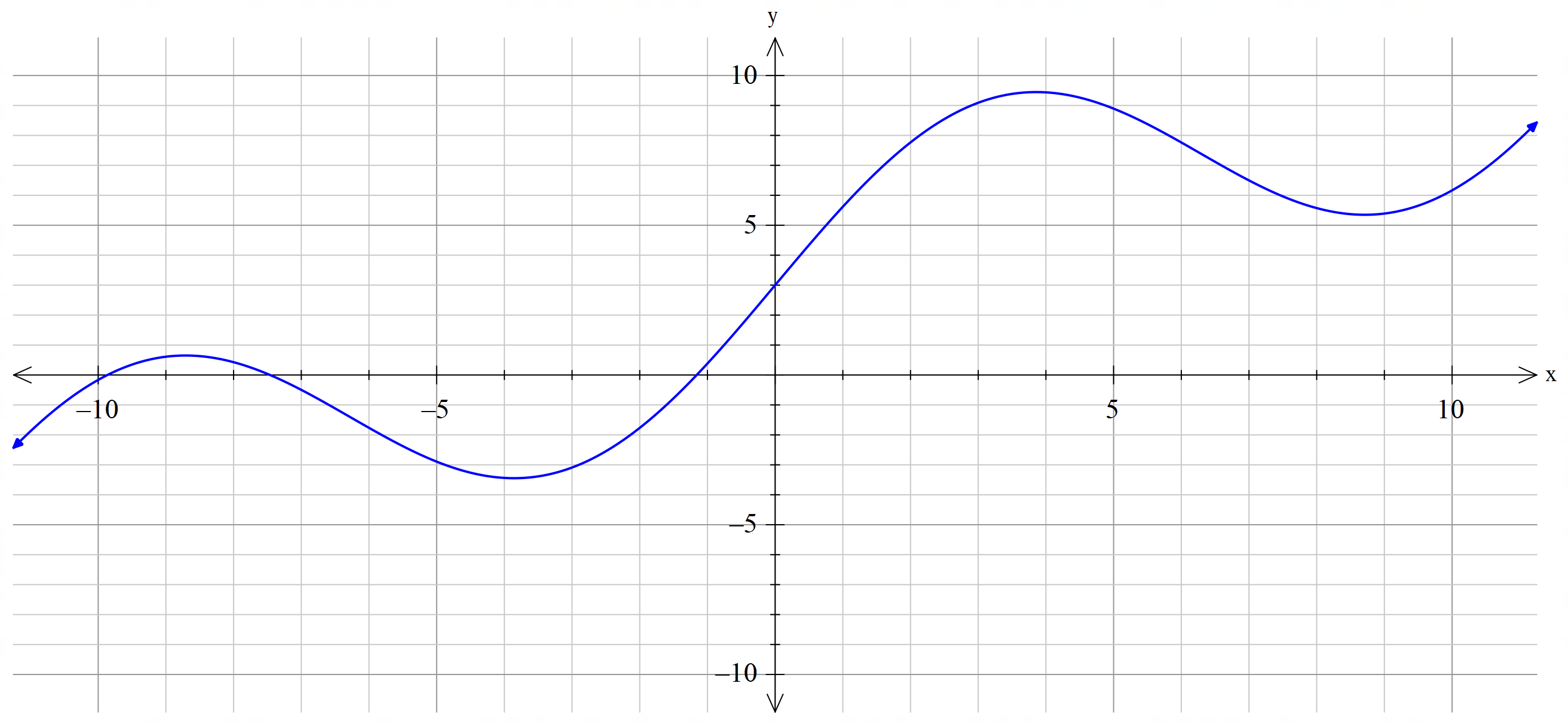
Determine the five roots of the equation



giving the answers in polar form with arguments  lying in the range .

**Question 8 (6 marks)**

The graph of is shown below.



Sketch on the same axes the graphs of

(a) (2 marks)

(b) (2 marks)

(c) (2 marks)

Make sure you distinguish clearly the three graphs.

**Additional working space**

Question number: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Additional working space**

Question number: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

**Acknowledgements**

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